Essential Tools for Scientific Machine Learning and Scientific Al				Comparison of tools readily usable with differentiable programming (automatic differentiation) frameworks			
Subject AD Frameworks	ADIFOR or TAF	ADOL-C	Stan	Julia (Zygote.jl, Tracker.jl, ForwardDiff.jl, etc.)	TensorFlow	PyTorch	Misc. other good packages
Language	Fortran	C++	Misc.	Julia	Python, Swift, Julia, etc.	Python	
Neural Networks	neural-fortran	OpenNN	None	Flux.jl	Built-in	Built-in	ADIFOR
Neural Differential Equations	Sundials (ODE+DAE)	Sundials (ODE+DAE)	Sundials (ODE+DAE)	DifferentialEquations.jl / DiffEqFlux.jl (ODE, SDE, DDE, DAE, hybrid, (S)PDE)	DifferentialEquations.jl (through Tensorflow.jl)	torchdiffeq (non-stiff ODEs)	PyMC3 (Python)
	FATODE	PETSC TS	Built-in (non-stiff ODE)	Sundials.jl (ODE through DiffEqFlux.jl)		diffeqpy	SMT (Python)
Probabilistic Programming	None	CPProb	Built-In	Gen.jl	Edward	Руго	sensitivity (R)
				Turing.jl	РуМС4	pyprob	ColPACK (Fortran)
Sparsity Detection	Built-in (TAF)	Built-in	None	SparsityDetection.jl	None	None	Dakota
Sparse Differentiation	Built-in (TAF)	Built-in	None	SparseDiffTools.jl	None	None	PSUDAE
GPU Support	CUDA	CUDA	OpenCL	CUDANative.jl + CuArrays.jl	Built-in	Built-in	Mondrian
Distributed Dense Linear Algebra	ScalAPACK	Elemental	None	Elemental.jl	Built-in	torch.distributed (no factorizations)	SimLab (MATLAB)
				DistributedArrays.jl		Elemental	Halide
Distributed Sparse Linear Algebra	ScalAPACK	PETSc	None	Elemental.jl	Built-in (no factorizations)	Elemental	dolfin-adjoint (AD for FEniCS/Firedrake)
				PETSo ii		petsc/py	
	PARASOL	Trilinos		i ciociji	None	репосчру	
	PARASOL	Trilinos Elemental			None	ревочру	
Structured Linear Algebra	PARASOL	Trilinos Elemental None	None	(Block)BandedMatrices.jl	None Some built-in	None	
Structured Linear Algebra	PARASOL SPARSEKIT None	Trilinos Elemental None MUQ	None	(Block)BandedMatrices.jl Surrogates.jl	None Some built-in None	None pySOT	
Structured Linear Algebra Surrogate Modeling Global Sensitivity Analysis	PARASOL SPARSEKIT None None	Trilinos Elemental None MUQ None	None None None	(Block)BandedMatrices.jl Surrogates.jl DifferentialEquations.jl / DiffEqSensitivity.jl	None Some built-in None None	None pySOT SALib	
Structured Linear Algebra Surrogate Modeling Global Sensitivity Analysis Uncertainty Quantification	PARASOL SPARSEKIT None None	Trilinos Elemental None MUQ None	None None None None	(Block)BandedMatrices.jl Surrogates.jl DifferentialEquations.jl / DiffEqSensitivity.jl DifferentialEquations.jl / DiffEqUncertainty.jl	None None None None None None None	None pySOT SALib uncertainpy	
Structured Linear Algebra Surrogate Modeling Global Sensitivity Analysis Uncertainty Quantification Direct Distributed Parallelism	PARASOL SPARSEKIT None None MPI	Trilinos Elemental None MUQ None MUQ MUQ	None None None None None None	(Block)BandedMatrices.jl Surrogates.jl DifferentialEquations.jl / DiffEqSensitivity.jl DifferentialEquations.jl / DiffEqUncertainty.jl MPI.jl	None Some built-in None None None Built-in	None None SALib Uncertainpy torch.distributed	
Structured Linear Algebra Surrogate Modeling Global Sensitivity Analysis Uncertainty Quantification Direct Distributed Parallelism PDE Discretizations	PARASOL SPARSEKIT None None None C++ Libraries w/ Fortran interfaces (hypre)	Trilinos Elemental None MUQ None MUQ deal.ii	None None None None None None None	<pre>(Block)BandedMatrices.jl (Block)BandedMatrices.jl Surrogates.jl DifferentialEquations.jl / DiffEqSensitivity.jl DifferentialEquations.jl / DiffEqUncertainty.jl MPI.jl ApproxFun.jl</pre>	None Some built-in None None None Built-in	None None SALID Uncertainpy FEniCS	
Structured Linear Algebra Surrogate Modeling Global Sensitivity Analysis Uncertainty Quantification Direct Distributed Parallelism PDE Discretizations	PARASOL SPARSEKIT None None None C++ Libraries w/ Fortran interfaces (hypre)	Trilinos Elemental None None None MUQ AUQ AUQ AUQ AUQ AUQ AUQ AUQ AUQ AUQ A	None None None None None	<pre>(Block)BandedMatrices.jl (Block)BandedMatrices.jl Surrogates.jl DifferentialEquations.jl / DiffEqSensitivity.jl DifferentialEquations.jl / DiffEqUncertainty.jl MPI.jl DiffEqOperators.jl</pre>	None Some built-in None None None Built-in	None None pySOT SALib uncertainpy torch.distributed FEniCS Firedrake	

Note: these statements/ratings are all about AD compatibility and usability for scientific machine learning and not necessarily applicable to traditional machine learning

For more details, see http://www.stochasticlifestyle.com/a-comparison-between-differential-equation-solver-suites-in-matlab-r-julia-python-c-and-fortran

Scale	None	Poor	Fair
Explanation	No automatic differentiation compatible library exists. Suggestion for a library to wrap.	Functionality exists, but is feature-incomplete or AD compatibility is incomplete. If no AD support, then AD support can easily be added since the library already defines adjoints.	The basic features exist, but has some major features missing or are not AD- compatible.

Excellent

Has all of the main features and is fully compatible with the automatic differentiation tooling.